

6th week

الأسبوع السادس

Resultant of non – concurrent force محصلة القوى غير الملتقية

To Find the resultant of non – concurrent forces

لإيجاد محصلة القوى غير الملتقية يجب إتباع الخطوات التالية :

1. we must solve the forces in to its components

تحلل القوى إلى مركباتها

2. we must find the resultant of components parallel to x - axis

(R_X) إيجاد محصلة المركبات الموازية لمحور السينات

3. we must find the resultant of components parallel to Y - axis

(R_Y) إيجاد محصلة المركبات الموازية لمحور الصادات

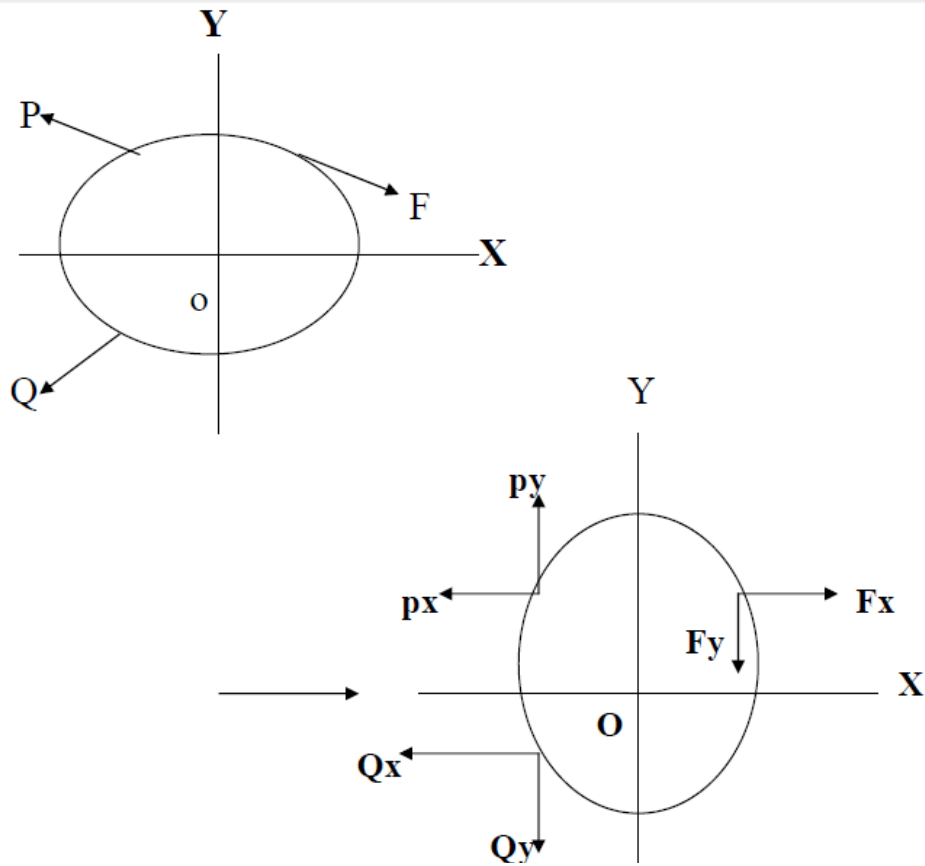
4. we must find R , θ , d

R = resultant المحصلة

θ = Direction of resultant اتجاه المحصلة

d = Distance of resultant بعد المحصلة

the following fig يوضح المعنى الشكل التالي shown there meaning



$$R_x = F_x - P_x - Q_x$$

$$R_y = p_y - F_y - Q_y$$

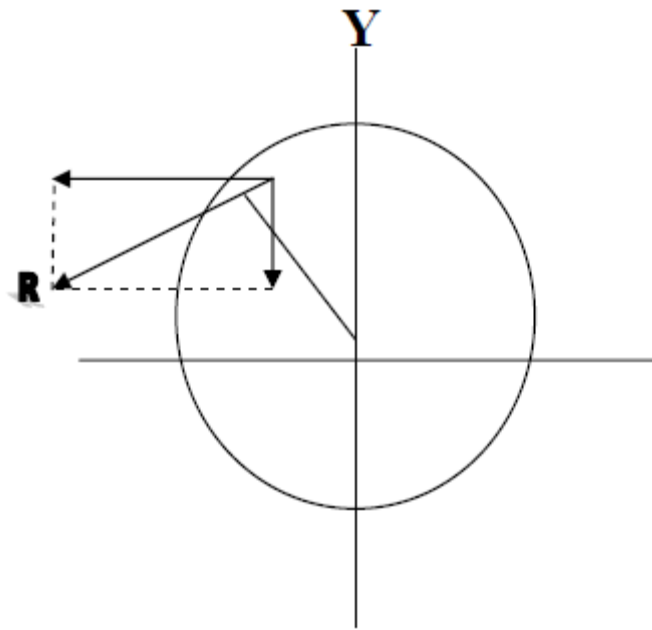
$$R = \sqrt{R_x^2 + R_y^2}$$

$$\tan \theta_x = \frac{R_y}{R_x}$$

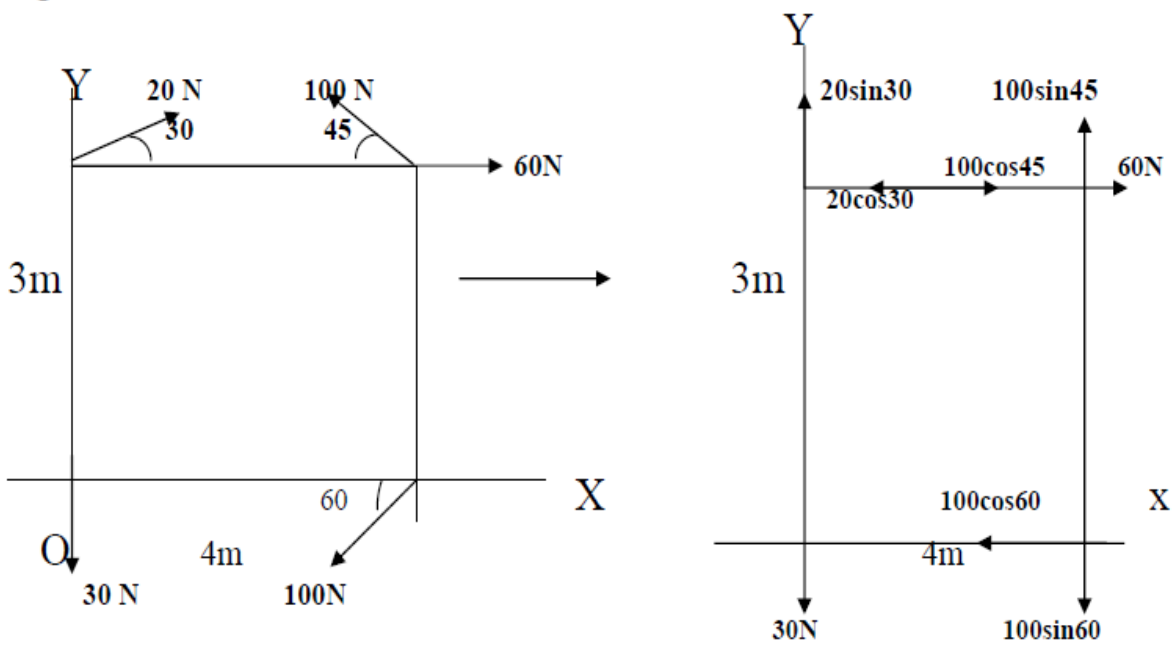
$\theta_x =$ ميل المحصلة عن محور السينات

$$R * d = \sum M_o$$

عزم المحصلة حول (O) = مجموع عزوم القوى حول (O)



Q// The rectangular framework shown in fig . is subjected to the indicated non – concurrent system of forces . determine the magnitude and direction of the resultant , also its arm relative to origin (O) .



$$R_X = 20 \cos 30 - 100 \cos 45 - 100 \cos 60 + 60$$

$$R_X = 20 * 0.866 - 100 * 0.707 - 100 * 0.5 + 60$$

$$R_X = 17.32 + 60 - 70.7 - 50$$

$$R_X = 43.38 \text{ N}$$

$$R_X = 43.38 \text{ N} \leftarrow$$

$$R_Y = 20 \sin 30 + 100 \sin 45 - 100 \sin 60 - 30$$

$$R_Y = 10 * 0.5 + 100 * 0.707 - 100 * 0.866 - 30$$

$$R_Y = -35.9 \text{ N}$$

$$R_Y = 35.9 \text{ N} \downarrow$$

$$R = \sqrt{R_X^2 + R_Y^2} = \sqrt{(43.38)^2 + (35.9)^2}$$

$$R = 56.3 \text{ N}$$

$$\tan \theta = \frac{R_Y}{R_X} = \frac{35.9}{43.38} = 0.827$$

$$\theta = 39.6$$

$$R * d = \sum M_o$$

$$R * d = (30 * 0) + (20 \cos 30 * 3) + (20 \sin 30 * 0) \\ - (100 \sin 45 * 4) - (100 \cos 45 * 3) + (60 * 3) \\ + (100 \sin 60 * 4) + (100 \cos 60 * 0)$$

$$R * d = 0 + 20 * 0.866 * 3 + 20 * 0.5 * 0 \\ + 100 * 0.707 * 4 + 100 * 0.707 * 3 + 180 + 100 * 0.866 * 4 + 100 * 0.5 * 0$$

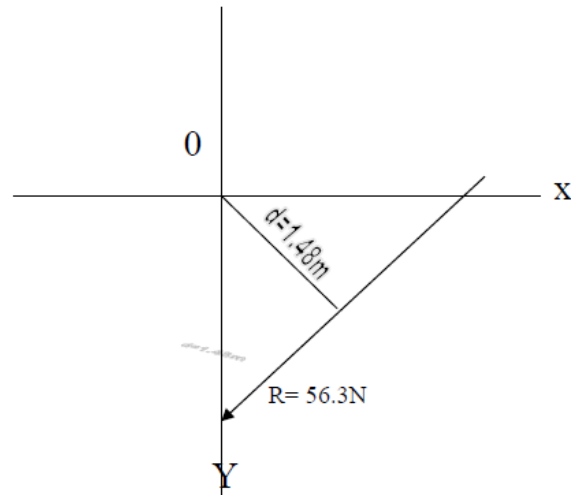
$$+ 100 * 0.866 * 4 + 100 * 0.5 * 0$$

$$R * d = 0 + 51.96 + 0 - 212.1 - 282.8 + 180 + 346.4 + 0$$

$$R * d = 83.46 \text{ N.m}$$

$$d = \frac{93.46}{56.3} = 1.48 \text{ m}$$

$$d = 1.48 \text{ m}$$



Q// Determine completely the resultant of force acting on step pulley shown in Fig .

$$R_x = 750 \cos 30 + 250$$

$$R_x = 750 * 0.866 + 250$$

$$R_x = 899.5 \text{ N}$$

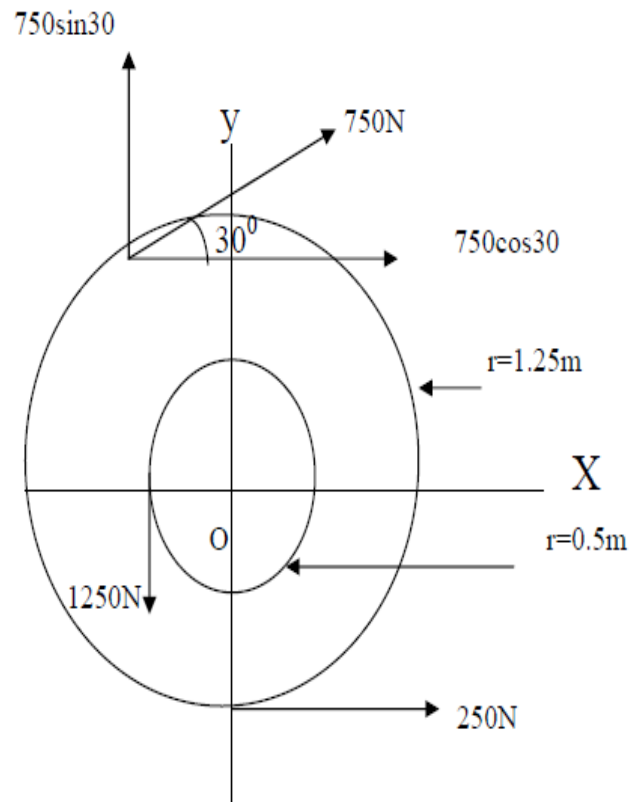
$$R_x = 899.5 \text{ N} \rightarrow$$

$$R_y = 750 \sin 30 - 1250$$

$$R_y = 750 * 0.5 -$$

$$R_y = - 875 \text{ N}$$

$$R_y = 875 \text{ N} \downarrow$$



$$R = \sqrt{R_x^2 + R_y^2} = \sqrt{(899.5)^2 + (875)^2}$$

$$R = 1255 \text{ N}$$

$$\tan \theta = \frac{R_y}{R_x} = \frac{875}{899.5} = 0.972$$

$$\theta = 44^\circ$$

$$R * d = \sum M_o$$

$$R * d = 750 * 1.25 - 1250 * 0.5 - 250 * 1.25$$

$$R * d = 0$$

$$d = 0$$

أي أن (R) تمر في النقطة (O) .