

5. Friction:

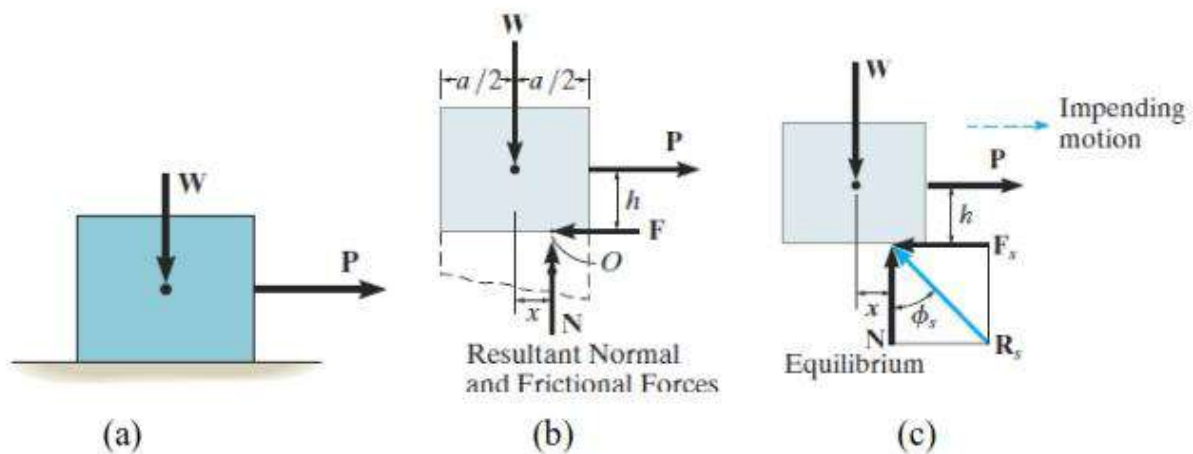
Friction is a force that resists the movement of two contacting surfaces that slide relative to one another.

Considering the effects caused by pulling horizontally force P on a block of uniform weight W which is resting on a rough horizontal surface. From equilibrium, two reaction forces generated;

Normal force N to resist the weight W and

Friction force F to resist the pulling force P .

Notice that N acts a distance x to the right of the line of action of W , Fig. (b) which coincides with geometric center of in order to balance the effect caused by P .



Impending Motion: If the block will tend to slip, the maximum value called the limiting static frictional force, Fig. (c), which is directly proportional to the resultant normal force N . Expressed mathematically:

$$F_s = \mu_s \cdot N$$

- Where: μ_s (mu "sub" s), is called the coefficient of static friction. Typical values for μ_s are given in Table 8-1.
- When the block is on verge of sliding, the normal force N and frictional force F_s create a resultant R_s Fig. (c).

The angle ϕ_s (phi "sub" s) that makes with N is called the angle of static friction.

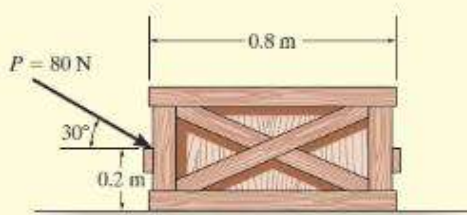
$$\phi_s = \tan^{-1}\left(\frac{F_s}{N}\right) = \tan^{-1}\left(\frac{\mu_s N}{N}\right) = \tan^{-1} \mu_s$$

Table 8-1
Typical Values for μ_s

Contact Materials	Coefficient of Static Friction (μ_s)
Metal on ice	0.03–0.05
Wood on wood	0.30–0.70
Leather on wood	0.20–0.50
Leather on metal	0.30–0.60
Aluminum on aluminum	1.10–1.70

Ex (1):

The uniform crate shown in Fig. 8-7a has a mass of 20 kg. If a force $P = 80 \text{ N}$ is applied to the crate, determine if it remains in equilibrium. The coefficient of static friction is $\mu_s = 0.3$.



(a)

Fig. 8-7

SOLUTION

Free-Body Diagram. As shown in Fig. 8-7b, the *resultant* normal force N_C must act a distance x from the crate's center line in order to counteract the tipping effect caused by \mathbf{P} . There are *three unknowns*, F , N_C , and x , which can be determined strictly from the *three* equations of equilibrium.

Equations of Equilibrium.

$$\rightarrow \Sigma F_x = 0; \quad 80 \cos 30^\circ \text{ N} - F = 0$$

$$+\uparrow \Sigma F_y = 0; \quad -80 \sin 30^\circ \text{ N} + N_C - 196.2 \text{ N} = 0$$

$$\zeta + \Sigma M_O = 0; \quad 80 \sin 30^\circ \text{ N}(0.4 \text{ m}) - 80 \cos 30^\circ \text{ N}(0.2 \text{ m}) + N_C(x) = 0$$

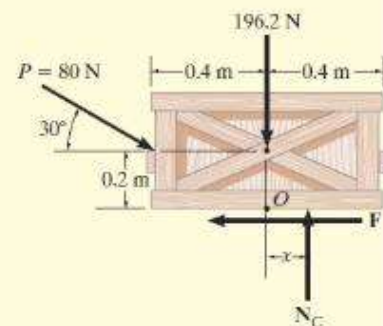
Solving,

$$F = 69.3 \text{ N}$$

$$N_C = 236 \text{ N}$$

$$x = -0.00908 \text{ m} = -9.08 \text{ mm}$$

Since x is negative it indicates the *resultant* normal force acts (slightly) to the *left* of the crate's center line. No tipping will occur since $x < 0.4 \text{ m}$. Also, the *maximum* frictional force which can be developed at the surface of contact is $F_{\max} = \mu_s N_C = 0.3(236 \text{ N}) = 70.8 \text{ N}$. Since $F = 69.3 \text{ N} < 70.8 \text{ N}$, the crate will *not slip*, although it is very close to doing so.



(b)

Ex (2):

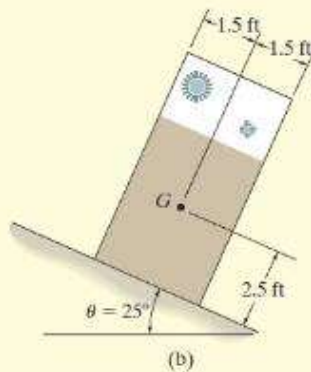


(a)

It is observed that when the bed of the dump truck is raised to an angle of $\theta = 25^\circ$ the vending machines will begin to slide off the bed, Fig. 8–8a. Determine the static coefficient of friction between a vending machine and the surface of the truckbed.

SOLUTION

An idealized model of a vending machine resting on the truckbed is shown in Fig. 8–8b. The dimensions have been measured and the center of gravity has been located. We will assume that the vending machine weighs W .



(b)

Free-Body Diagram. As shown in Fig. 8–8c, the dimension x is used to locate the position of the resultant normal force N . There are four unknowns, N , F , μ_s , and x .

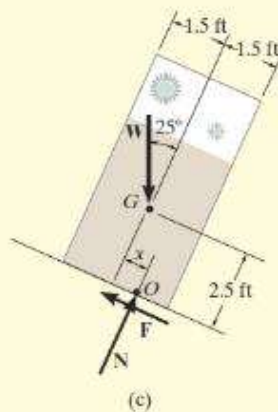
Equations of Equilibrium.

$$\begin{aligned}
 +\curvearrowright \Sigma F_x = 0; & \quad W \sin 25^\circ - F = 0 & (1) \\
 +\nearrow \Sigma F_y = 0; & \quad N - W \cos 25^\circ = 0 & (2) \\
 \zeta + \Sigma M_O = 0; & \quad -W \sin 25^\circ(2.5 \text{ ft}) + W \cos 25^\circ(x) = 0 & (3)
 \end{aligned}$$

Since slipping impends at $\theta = 25^\circ$, using Eqs. 1 and 2, we have

$$\begin{aligned}
 F_s = \mu_s N; & \quad W \sin 25^\circ = \mu_s(W \cos 25^\circ) \\
 \mu_s = \tan 25^\circ = 0.466 & \quad \text{Ans.}
 \end{aligned}$$

The angle of $\theta = 25^\circ$ is referred to as the *angle of repose*, and by comparison, it is equal to the angle of static friction, $\theta = \phi_s$. Notice from the calculation that θ is independent of the weight of the vending machine, and so knowing θ provides a convenient method for determining the coefficient of static friction.



(c)

Fig. 8–8

NOTE: From Eq. 3, we find $x = 1.17 \text{ ft}$. Since $1.17 \text{ ft} < 1.5 \text{ ft}$, indeed the vending machine will slip before it can tip as observed in Fig. 8–8a.

Ex (3):

The uniform 10-kg ladder in Fig. 8-9*a* rests against the smooth wall at *B*, and the end *A* rests on the rough horizontal plane for which the coefficient of static friction is $\mu_s = 0.3$. Determine the angle of inclination θ of the ladder and the normal reaction at *B* if the ladder is on the verge of slipping.

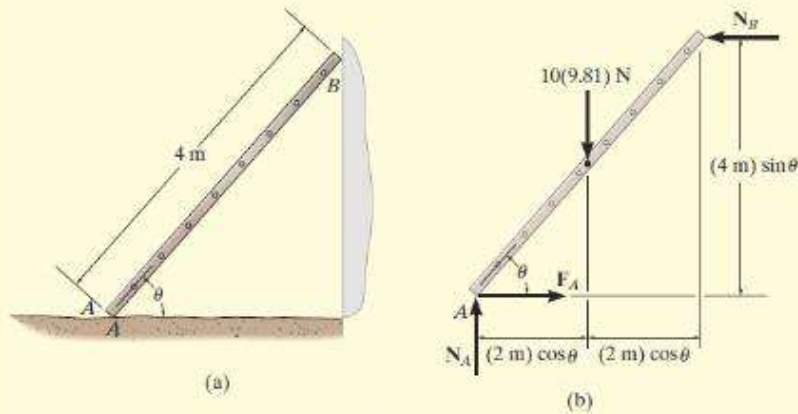


Fig. 8-9

SOLUTION

Free-Body Diagram. As shown on the free-body diagram, Fig. 8-9*b*, the frictional force F_A must act to the right since impending motion at *A* is to the left.

Equations of Equilibrium and Friction. Since the ladder is on the verge of slipping, then $F_A = \mu_s N_A = 0.3N_A$. By inspection, N_A can be obtained directly.

$$+\uparrow \Sigma F_y = 0; \quad N_A - 10(9.81) \text{ N} = 0 \quad N_A = 98.1 \text{ N}$$

Using this result, $F_A = 0.3(98.1 \text{ N}) = 29.43 \text{ N}$. Now N_B can be found.

$$\begin{aligned} \rightarrow \Sigma F_x = 0; \quad 29.43 \text{ N} - N_B &= 0 \\ N_B &= 29.43 \text{ N} = 29.4 \text{ N} \quad \text{Ans.} \end{aligned}$$

Finally, the angle θ can be determined by summing moments about point *A*.

$$\begin{aligned} \curvearrowright \Sigma M_A = 0; \quad (29.43 \text{ N})(4 \text{ m}) \sin \theta - [10(9.81) \text{ N}](2 \text{ m}) \cos \theta &= 0 \\ \frac{\sin \theta}{\cos \theta} = \tan \theta &= 1.6667 \\ \theta &= 59.04^\circ = 59.0^\circ \quad \text{Ans.} \end{aligned}$$

Q/ The (200N) block shown in Fig . Has impending motion up the plane . Caused by $\text{على وشك الحركة على السطح}$ the Horizontal force قوة افقية of (400N) .

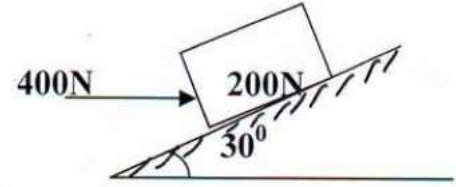
Determine the coefficient of static friction between the contact surfaces السطوح المتلامسة .

هنا اتزان القوى الملتقية

$$R_x = 0 \quad , \quad R_y = 0$$

$$F = 400 * 0.866 - 200 * 0.5$$

$$R_x = 400 \cos 30 - 200 \cos 60 - F = 0$$



$$F = 246.4 \text{ N}$$

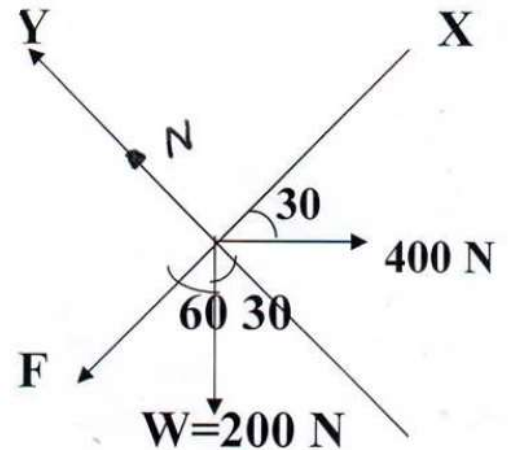
$$R_y = 0$$

$$N - 200 \sin 60 - 400 \sin 30 = 0$$

$$N = 200 * 0.866 + 400 * 0.5$$

$$N = 173.2 + 200$$

$$N = 373.2 \text{ N}$$



نأخذ سطوح التلامس هو X . axis

$$F = f * N$$

$$f = \frac{F}{N} = \frac{246.4}{373.2} = 0.66$$

f = معامل الاحتكاك خالي من الوحدات =