

Equilibrium of force system اتزان نظام القوى

Definition and meaning of equilibrium تعريف ومعنى الاتزان

Such bodies في حالة اتزان بعض الاجسام are said to be يقال انها in equilibrium

Equilibrium الاتزان is the term مصطلح used يستخدم to designate وصف the condition حال where the resultant محصلة القوى of system of force is zero . A body is said to be in equilibrium when Resultant محصلة of force system نظام القوى acting on body is zero – the physical meaning المعنى الفيزيائي of equilibrium the body either أما at (rest) or moving on straight line يتحرك على خط مستقيم with constant velocity سرعة ثابتة .

Equilibrium of concurrent forces اتزان القوى الملتقية

When the concurrent forces are in equilibrium the resultant of concurrent force is zero ($R = 0$)

So we applied .

$$R_x = 0$$

$$R_y = 0$$

Equilibrium of none concurrent forces اتزان القوى غير الملتقية

When the none concurrent forces are in equilibrium the resultant of the non concurrent forces is zero ($R = 0$) . so we

applied there equation to solve problem .


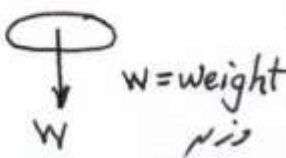
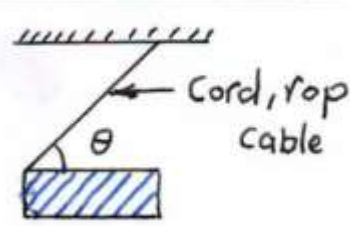
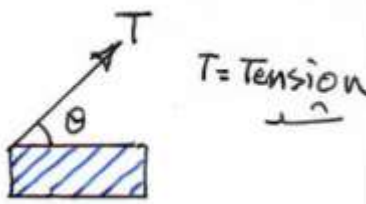
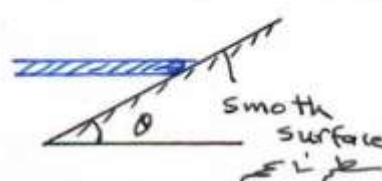
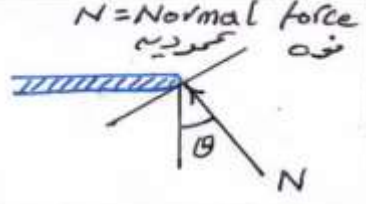
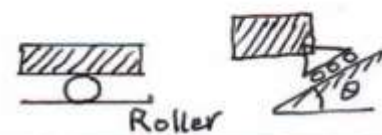
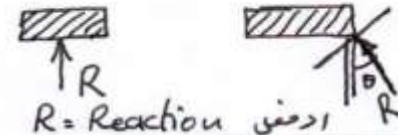


$$R_x = 0$$

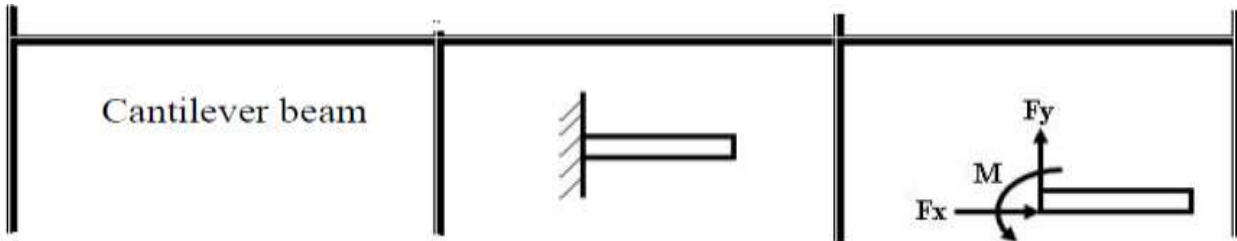
$$R_y = 0$$

$$\sum M = 0$$

Free body Diagram رسم الجسم الحر

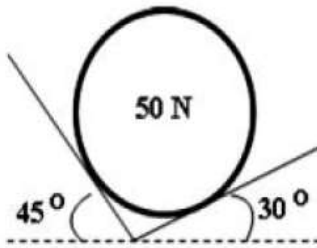
Problems in mechanics always involve the interaction of bodies on one another. A successful solution of these problems generally requires that the bodies be isolated from one another so that the forces involved may be analyzed and unknown forces determined. An isolated view of body is called a free body diagram (F . B . D)

Type of body removed نوع الجسم المحذوف	Sketch of reacting bodies رسم الاجسام المتصلة	Acting of a body removed up on free body تأثير الجسم المحذوف على الجسم المعزول
Earth الارض		 $W = \text{weight}$ وزن
Cord وتر Rope حبل Cable حبل معدني (weight is neglected) وزنه محذوف		 $T = \text{Tension}$ شد
Smooth surface سطح ناعم		 $N = \text{Normal force}$ قوة عمودية سطح ناعم
Roller رولة أو اسطوانة		 $R = \text{Reaction}$ رد فعل
Smooth pin بيم		

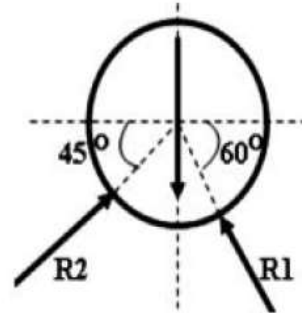


Ex (1):

Draw Free – body diagram for the 50 N sphere shown in fig.

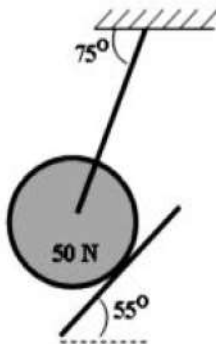


Solution

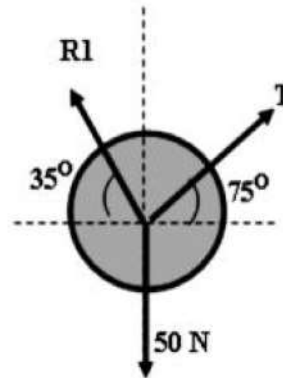


Ex (2):

Draw Free – body diagram for the 50 N sphere shown in fig.

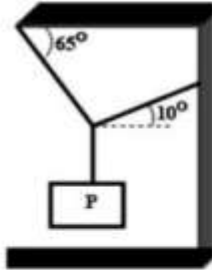


Solution

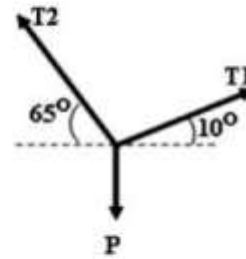


Ex (3):

Draw Free – body diagram for the ropes system shown in fig.

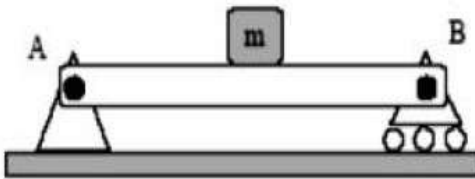


Solution

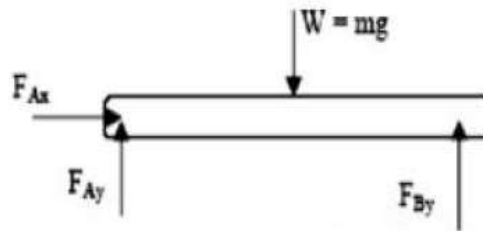


Examples

Mass at mid-point on beam (length L)



Free body diagram



Q// If the concurrent forces shown in Fig are in equilibrium find (F) And (θ) .

بما ان القوى الملتقية في حالة اتزان لذا فان (R = 0)

$$R_X = 0 \quad R_Y = 0$$

$$R_X = 0$$

$$400 \cos 30 + F \cos \theta - 300 = 0$$

$$F \cos \theta = 300 - 400 * 0.866$$

$$F \cos \theta = 300 - 346.4$$

$$F_X = F \cos \theta = - 46.4 \text{ N}$$

$$F_X = 46.4 \text{ N} \leftarrow$$

$$R_Y = 0$$

$$400 \sin 30 - F \sin \theta = 0$$

$$F \sin \theta = 400 * 0.5$$

$$F_Y = F \sin \theta = 200 \text{ N}$$

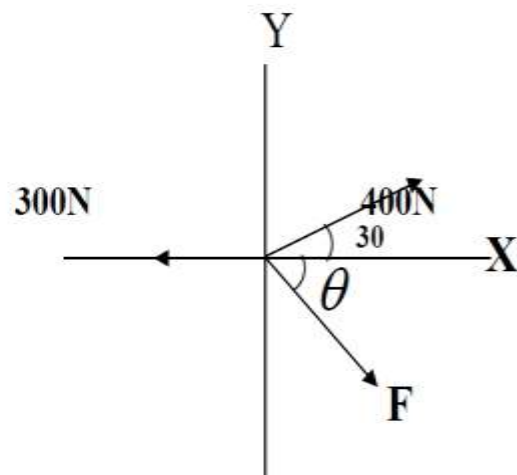
$$F_Y = 200 \text{ N} \uparrow$$

$$\tan \theta = \frac{F_Y}{F_X}$$

$$\tan \theta = \frac{200}{46.4}$$

$$\tan \theta = 4.31$$

$$\theta = 76.9^\circ$$

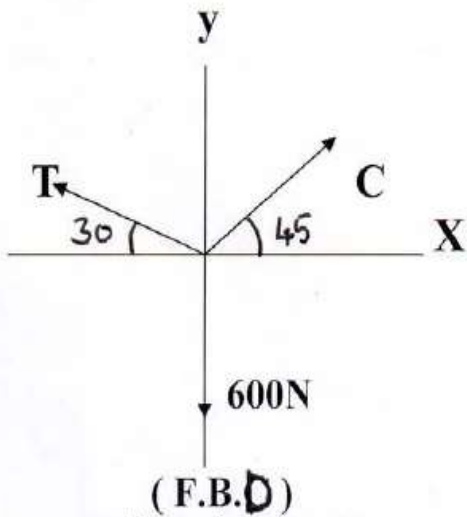


$$F = \sqrt{F_X^2 + F_Y^2}$$

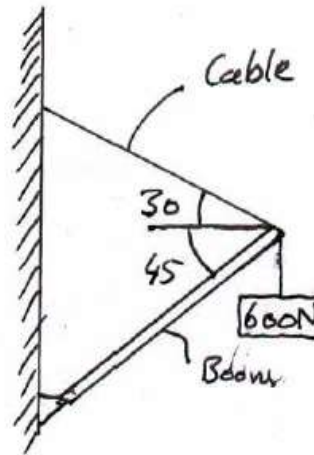
$$F = \sqrt{(46.4)^2 + (200)^2}$$

$$F = 205 \text{ N}$$

Q/ The cable **حبل معدني** and Boom **ذراع الرافعة** shown in Fig .
 Support a load of (600N) . **دetermine** **أحسب** the tensile force **قوة الشد** (T) in the cable and compressive force **قوة الضغط** (C) in the Boom **ذراع الرافعة** .when the system is in aquarium ?



بما ان النظام في حالة اتزان



$R = 0$
 $R_x = 0$, $R_y = 0$ لان القوى ملتقية

$R_x = 0$
 $C \cos 45 - T \cos 30 = 0$
 $C \cos 45 = T \cos 30$

$C = \frac{T * 0.866}{0.707} \rightarrow (1)$

$R_y = 0$
 $C \sin 45 + T \sin 30 - 600 = 0$

من ١

$\frac{T * 0.866}{0.707} * 0.707 + 0.5T = 600$

$0.866T + 0.5 T = 600$

$1.366T = 600$

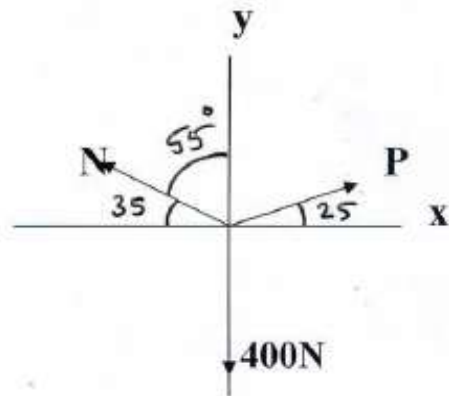
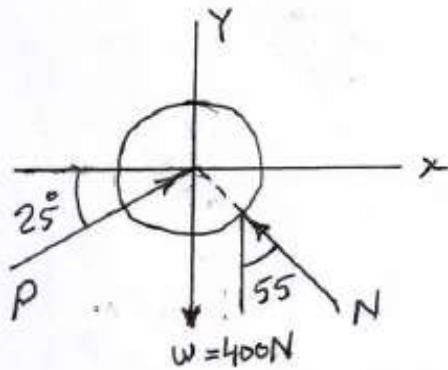
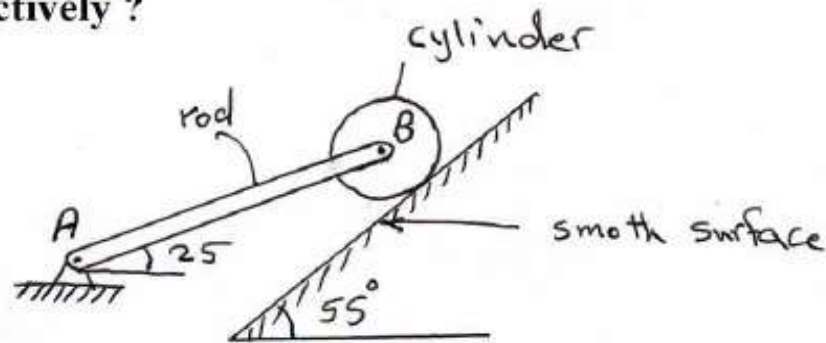
T = 439 N

نعوض في ١

$C = \frac{439 * 0.866}{0.707}$

C = 538 N

Q/ A cylinder (400N) is held against a smooth incline by means of the weightless rod (AB) as show in Fig . Determine the force (P) and (N) exerted on the cylinder by the rod (AB) and the incline respectively ?



بما ان القوى ملتقية وفي حالة اتزان

$$R = 0$$

$$R_x = 0 \quad R_y = 0$$

$$R_x = 0$$

$$P \cos 25 - N \cos 35 = 0$$

$$0.906 = 0.819 N$$

$$P = \frac{0.819}{0.906} N$$

$$P = 0.903 N \quad \text{--- (1)}$$

$$R_y = 0$$

$$P \sin 25 + N \sin 35 - 400 = 0$$

$$0.903 * 0.423 + 0.574 = 400$$

$$0.954 N = 400$$

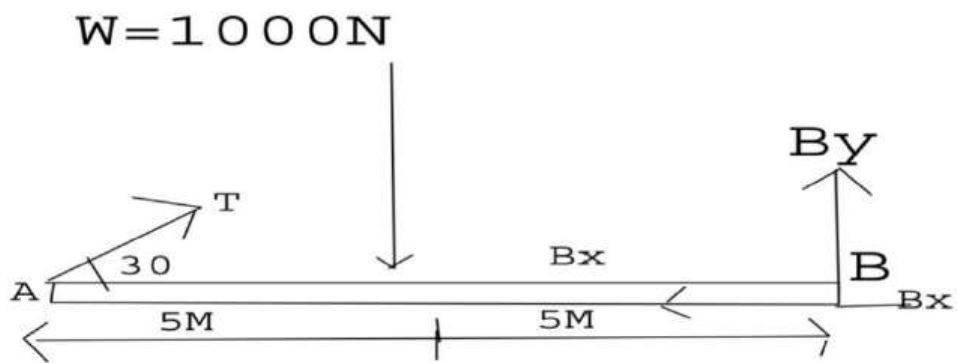
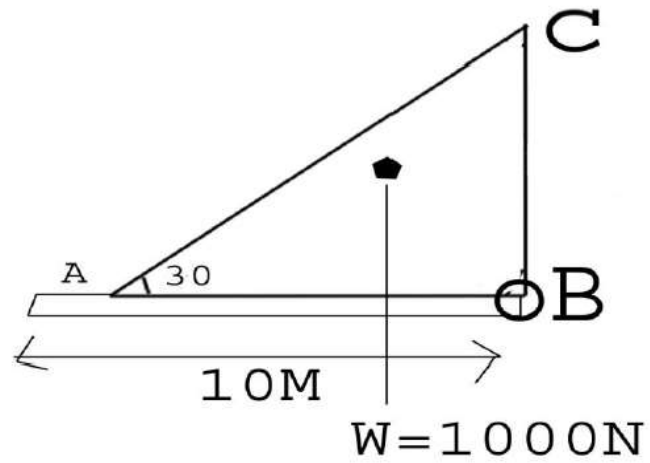
$$N = \frac{400}{0.954}$$

$$N = 419 N$$

$$P = 0.903 * 419 \quad \text{من 1}$$

$$P = 378 N$$

The bar (AB) weight (1000)N and is supported by a cable (AC) and a pin c at (B). Determine the reaction at (B) and the tension in the cable?



$$\Sigma MA=0 = -1000(5) + By(10)$$

$$By = 5000/10 = 500 \text{ N.m}$$

$$Ry = 0 = -1000 + By + T \sin 30^{\circ}$$

$$-1000 + 500 + T(0.5) = 0$$

$$T = 1000 \text{ N}$$

$$Rx = 0 = -Bx + T \cos 30^{\circ}$$

$$Bx = 1000(0.866)$$

$$Bx = 866 \text{ N}$$